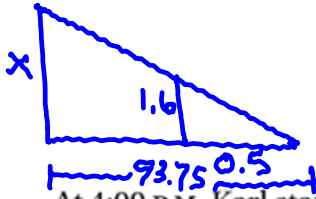


## Similarity in Right Triangles and Proportion

### Warm-up:

- 1) A 1.6-m-tall woman stands next to the Eiffel Tower. At this time of day, her shadow is 0.5 m long. At the same time, the tower's shadow is 93.75 m long. How tall is the Eiffel Tower?

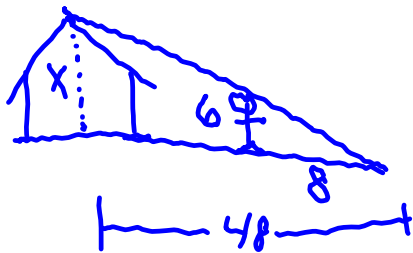


$$\frac{0.5}{93.75} = \frac{1.6}{x}$$

$$0.5x = 150$$

$$x = 300 \text{ m}$$

- 2) At 4:00 P.M. Karl stands next to his house and measures his shadow and the house's shadow. Karl's shadow is 8 ft long. The house's shadow is 48 ft long. If Karl is 6 ft tall, how tall is his house?



$$\frac{8}{48} = \frac{6}{x}$$

$$\frac{1}{6} = \frac{6}{x}$$

$$x = 36 \text{ ft.}$$

# Homework Check

Proving Triangles Similar WS #12-15

# Similarity in Right Triangles and Proportion

Homework:

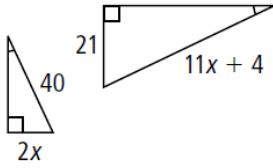
$$\frac{2x}{21} = \frac{40}{11x+4}$$

$$22x^2 + 8x = 840$$

$$22x^2 + 8x - 840 = 0$$

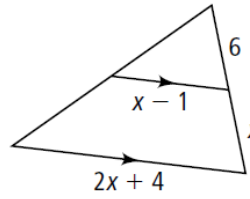
Algebra Explain why the triangles are similar. Then find the value of  $x$ .

12.



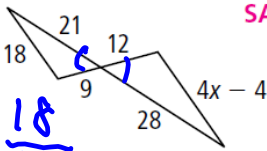
AA ~ Post.; 6

13.



AA ~ Post.; 10

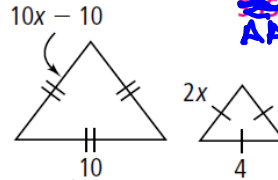
14.



SAS ~ Thm.; 7

$$\frac{18}{9} = \frac{21}{4x-4}$$

15.



AA ~ Thm.; 2

$$2x = 4$$

$$x = 2$$

## Similarity in Right Triangles

Take note

### Theorem 62

**Theorem**

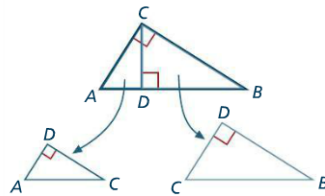
The altitude to the hypotenuse of a right triangle divides the triangle into two triangles that are similar to the original triangle and to each other.

**If ...**

$\triangle ABC$  is a right triangle with right  $\angle ACB$ , and  $\overline{CD}$  is the altitude to the hypotenuse

**Then ...**

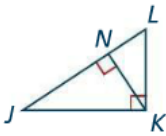
$\triangle ABC \sim \triangle ACD$   
 $\triangle ABC \sim \triangle CBD$   
 $\triangle ACD \sim \triangle CBD$



## Similarity in Right Triangles and Proportion

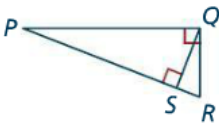
**Practice** Write a similarity statement relating the three triangles in each diagram.

1.



$$\begin{aligned} \triangle LJK &\sim \triangle KLN \\ \triangle LJK &\sim \triangle JKN \\ \triangle KLN &\sim \triangle JKN \end{aligned}$$

2.



$$\begin{aligned} \triangle PRQ &\sim \triangle QRS \\ \triangle PRQ &\sim \triangle QPS \\ \triangle QRS &\sim \triangle QPS \end{aligned}$$

## Proportions in Triangles

Take note

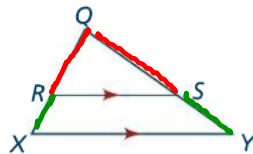
### Theorem 63 Side-Splitter Theorem

#### Theorem

If a line is parallel to one side of a triangle and intersects the other two sides, then it divides those sides proportionally.

#### If ...

$$\overleftrightarrow{RS} \parallel \overleftrightarrow{XY}$$



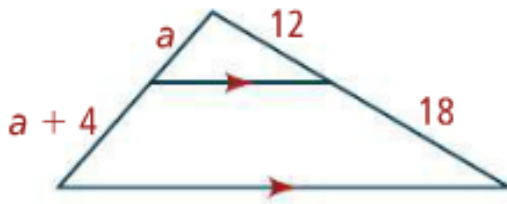
#### Then ...

$$\frac{XR}{RQ} = \frac{YS}{SQ}$$

## Similarity in Right Triangles and Proportion

### Problem 1 Using the Side-Splitter Theorem

What is the value of  $a$  in the diagram below?



$$\begin{aligned} \frac{12}{18} &= \frac{a}{a+4} \\ \frac{2}{3} &= \frac{a}{a+4} \end{aligned} \rightarrow \begin{aligned} 3a &= 2a + 8 \\ a &= 8 \end{aligned}$$

Take note

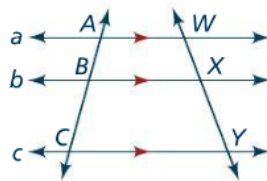
### Corollary Corollary to the Side-Splitter Theorem

#### Corollary

If three parallel lines intersect two transversals, then the segments intercepted on the transversals are proportional.

If ...

$$a \parallel b \parallel c$$



Then ...

$$\frac{AB}{BC} = \frac{WX}{XY}$$

## Similarity in Right Triangles and Proportion

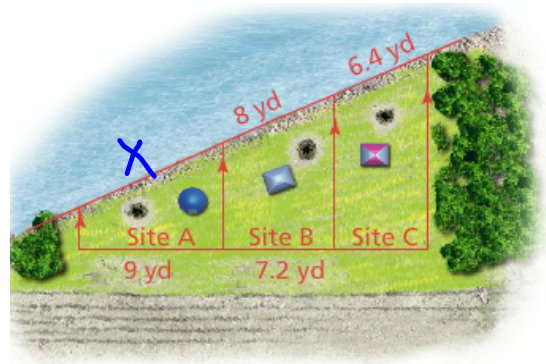
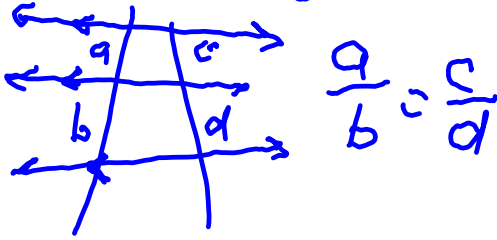
### Problem 2 Finding a Length

**Camping** Three campsites are shown in the diagram.  
What is the length of Site A along the river?

$$\frac{7.2}{9} = \frac{8}{x}$$

$$7.2x = 72$$

$$x = 10 \text{ yd.}$$



Practice

# Similarity in Right Triangles and Proportion

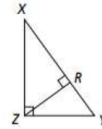
## Practice

Form K

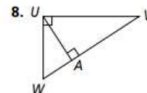
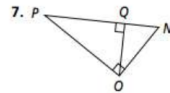
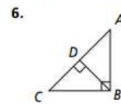
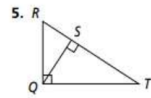
### Similarity in Right Triangles

Identify the following in right  $\triangle XYZ$ .

- the hypotenuse
- the segments of the hypotenuse
- the altitude to the hypotenuse
- the segment of the hypotenuse adjacent to leg  $\overline{ZY}$



Write a similarity statement relating the three triangles in each diagram.



## Practice

Form K

### Proportions in Triangles

Use the figure at the right to complete each proportion.

1.  $\frac{CE}{CF} = \frac{AC}{AI}$

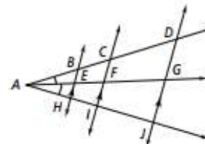
2.  $\frac{AB}{BC} = \frac{\square}{HI}$

3.  $\frac{\square}{IJ} = \frac{BC}{HI}$

4.  $\frac{JG}{\square} = \frac{GD}{AD}$

5.  $\frac{EG}{EF} = \frac{CD}{\square}$

6.  $\frac{AC}{AI} = \frac{\square}{IJ}$



Algebra Solve for  $x$ .

